

UNIVERSIDADE DE SÃO PAULO  
ESCOLA POLITÉCNICA – DEPARTAMENTO DE ENGENHARIA MECÂNICA

PME3380 – Modelagem de Sistemas Dinâmicos

## **Exercícios 12/11**

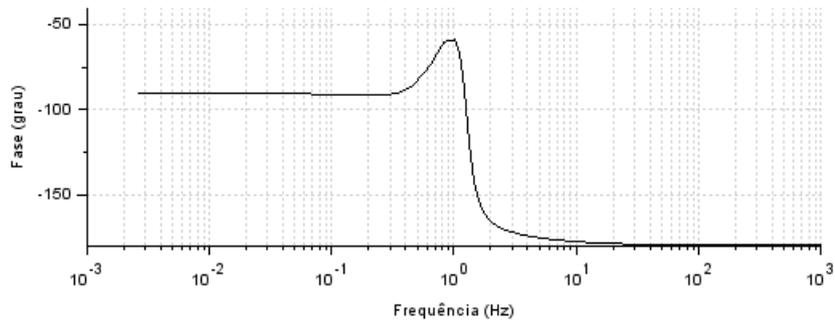
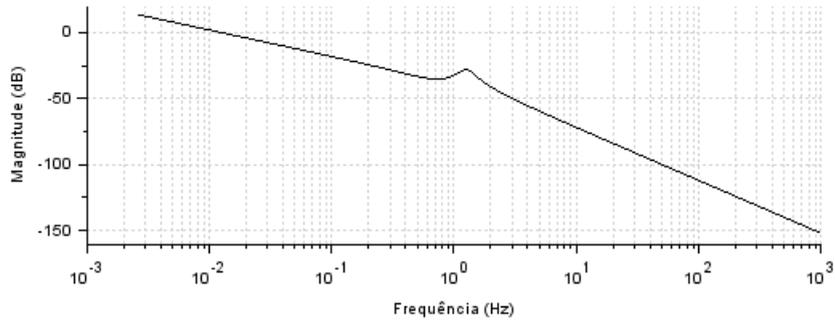
Pedro Leonel Giannoni de Oliveira

Número USP: 10335569

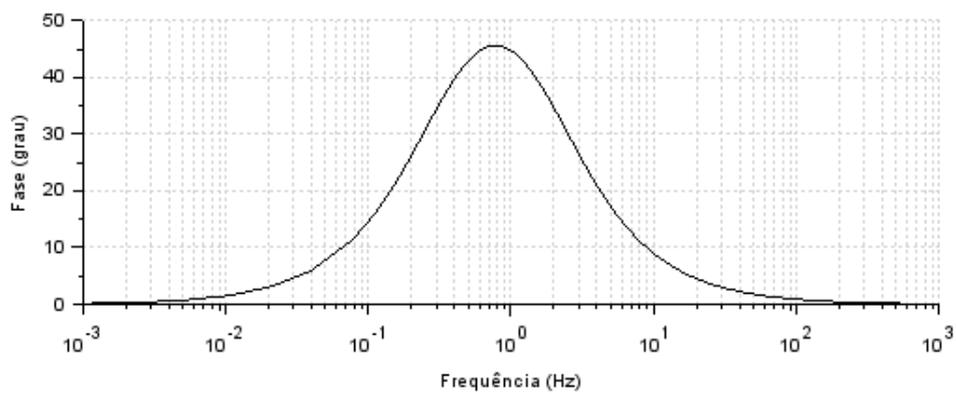
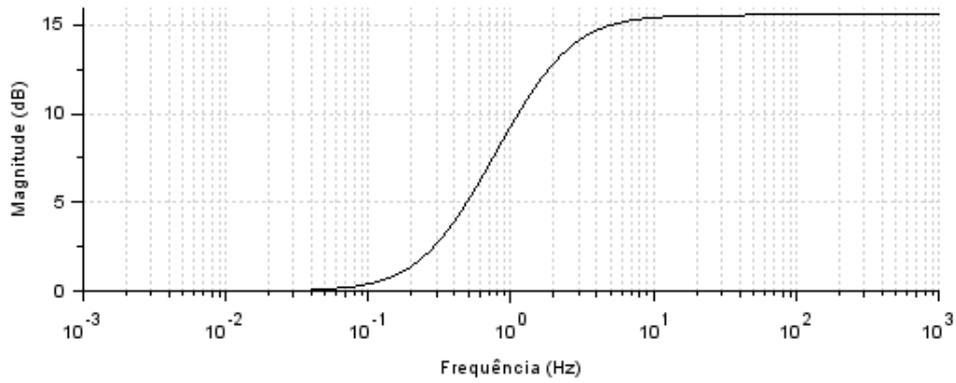
São Paulo

2020

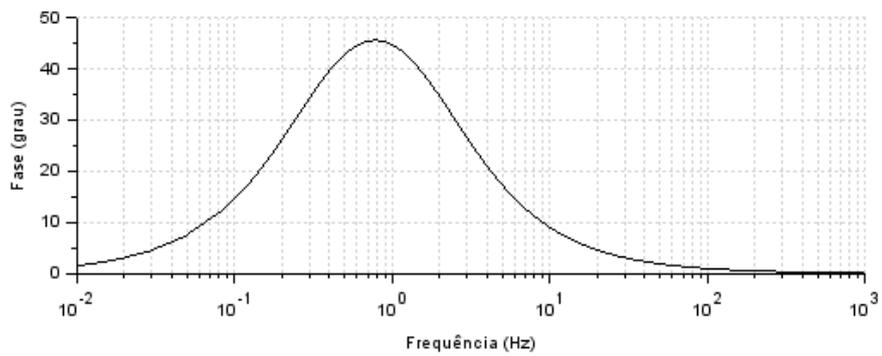
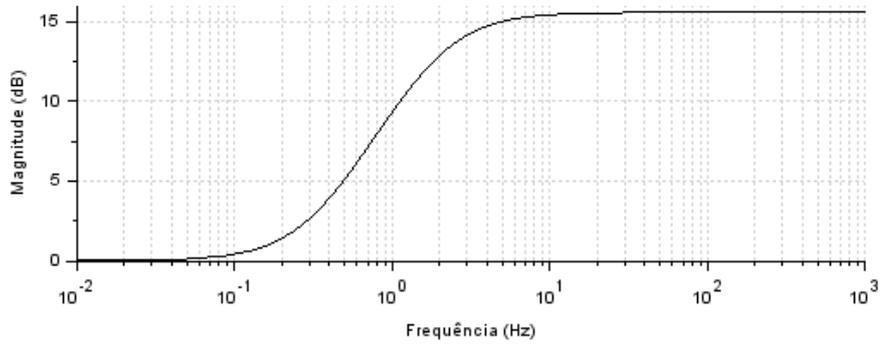
## Exercício 1



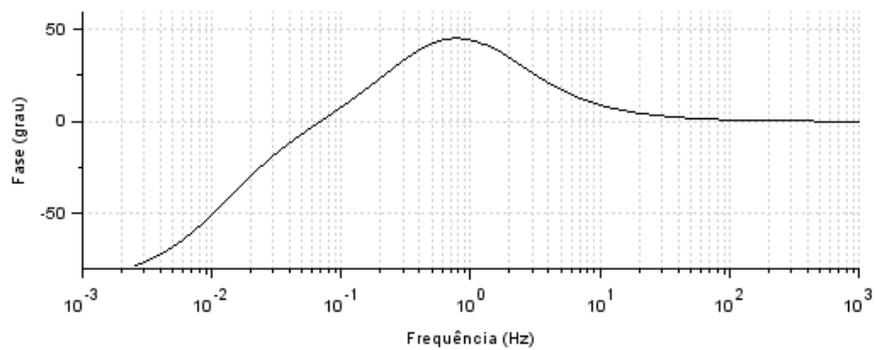
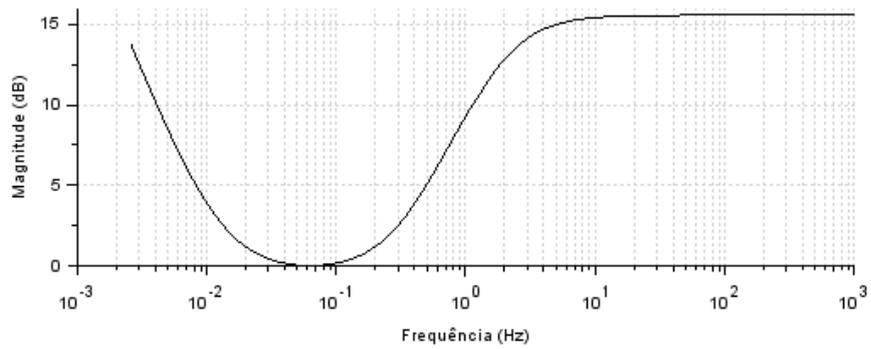
## Exercício 2



### Exercício 3



### Exercício 6



Exercícios 12/11 - Feito em scilab

$$1) G_1(s) = \frac{s^2 + 5s + 25}{s^4 + 7,4s^3 + 76s^2 + 320s}$$

$$2) G_2(s) = 6 \cdot \frac{(s+2)}{(s+12)}$$

3) A fase em 5 rad/s é de  $\approx 45^\circ$ 

4) Diagrama na última página

$$\bullet) \omega_n = \sqrt{1,2^2 + 7,9^2} = 7,99 \text{ rad/s}$$

$$\bullet) \zeta = \frac{1,2}{7,99} = 0,15$$

$$\bullet) \text{Pólos: } \left\{ \begin{array}{l} P_1 = -5 \\ P_2 = 0 \\ P_3 = -1,2 + 7,9j \\ P_4 = -1,2 - 7,9j \end{array} \right\} \text{ Dominantes}$$

$$\bullet) \omega_r = \omega_n \sqrt{1 - 2\zeta^2}$$

$$\Rightarrow \omega_r = 7,8 \text{ rad/s}$$

 $\bullet) \text{ Pico de ressonância em } 7,8 \text{ rad/s (esperado)}$ 
 $\bullet) \text{ Fase em } 5 \text{ rad/s é de } -62,3^\circ$ 

$$5) M_p = e^{\left( \frac{-\zeta \pi}{\sqrt{1 - \zeta^2}} \right)} = 62\%$$

 $6) \bullet) \text{ Fase em } 5 \text{ rad/s de } -16,8^\circ \text{ (soma das fases dos FTs)}$ 
 $\bullet) G_2 \text{ e } G_1 \text{ em série: magnitude aumenta em } \approx 15 \text{ dB após } 5 \text{ rad/s}$