

Ex 3/11 - 10772672 - Henrique Kuhlmann

$$\left. \begin{aligned} 1) \quad Y &= (I+GH)^{-1} G R \\ Y &= TR \end{aligned} \right\} T = (I+GH)^{-1} G$$

Pelo diagrama do slide 8:

$$\left. \begin{aligned} Z &= HY \\ R - E' &= HY \\ R - G^{-1}Y &= HY \end{aligned} \right\} \begin{aligned} (I+HG)^{-1}R &= G^{-1}Y \\ Y &= G(I+HG)^{-1}R \\ Y &= TR \end{aligned} \quad \left. \right\} T = G(I+HG)^{-1}$$

$$R = HY + G^{-1}Y \text{ (Algebra)}$$

$$R = (H + G^{-1})Y$$

$$R = (I + HG)G^{-1}Y$$

$$\text{Logo: } (I+GH)^{-1}G = G(I+HG)^{-1} = G(I+L)^{-1} = (I+L)^{-1}G$$

$$\text{Pois } L \equiv HG$$

$$2) \text{ a) } Z = HY$$

$$Z = HGE'$$

$$Z = HG(R-Z)$$

$$(I+HG)Z = HGR$$

$$Z = (I+HG)^{-1}HGR$$

$$b) \quad Y = GE'$$

$$H^{-1}Z = G(R-Z)$$

$$(H^{-1}+G)Z = GR$$

$$(I+GH)H^{-1}Z = GR$$

$$Z = H(I+GH)^{-1}GR$$

slide
está
errado!

Para o caso escalar, basta tratar as variáveis com escalares
e fazer $HG = GH = L$

$$3) Y = GH \cdot C$$

$$Y = GH \cdot (A - Y)$$

$$Y = GH \cdot R \cdot \frac{1}{H} - GH Y$$

$$(1 + GH)Y = GR$$

$$\boxed{\frac{Y}{R} = \frac{G}{1 + GH}}$$

$$Y = GE$$

$$Y = G(R - Z)$$

$$Y = G(R - YH)$$

$$Y(1 + HG) = GR$$

$$\boxed{\frac{Y}{R} = \frac{G}{1 + HG}} \checkmark$$

$$4) Y = \frac{G}{1 + G(H-1)} (R - Y) \sim Y \left(\frac{1 + G}{1 + G(H-1)} \right) = GR$$

$$\boxed{\frac{Y}{R} = \frac{G}{1 + GH}} \checkmark$$

$$5) G[(R - Y) - (H - 1)Y] = Y$$

$$G(R - HY) = Y$$

$$GR - GHY = Y$$

$$Y(1 + GH) = GR$$

$$\rightarrow \boxed{\frac{Y}{R} = \frac{G}{1 + GH}}$$

$$6) G[R - (H - 1)Y - Y] = Y$$

$$G(R - HY) = Y$$

$$GR - GHY = Y$$

$$\rightarrow \boxed{\frac{Y}{R} = \frac{G}{1 + GH}}$$

Product

$$7) D = 0 \sim (R - Y_1) G_1 G_2 = Y_1$$

$$G_1 G_2 R = Y_1 (1 + G_1 G_2)$$

$$\boxed{Y_1 = \frac{G_1 G_2 R}{1 + G_1 G_2}}$$

$$8) R = 0 \sim G_2 (D - G_1 Y_2) = Y_2$$

$$G_2 D - G_1 G_2 Y_2 = Y_2$$

$$Y_2 (1 + G_1 G_2) = G_2 D$$

$$\rightarrow \boxed{Y_2 = \frac{G_2 D}{1 + G_1 G_2}}$$

9) Com $R \neq 0 \neq D$

$$G_2 [G_1(R - Y) + D] = Y$$

$$G_1 G_2 R - G_1 G_2 Y + G_2 D = Y$$

$$Y(1 + G_1 G_2) = G_1 G_2 R + G_2 D \quad - Y = \frac{G_1 G_2 R}{1 + G_1 G_2} + \frac{G_2 D}{1 + G_1 G_2}$$

$$Y = Y_1 + Y_2 \quad (\text{do ex. 7 e 8})$$

Note que as funções de transferência apresentam os mesmos polos!

$$10) Z = W \pm X \pm Y \quad \equiv \quad Z = W + (\pm Y \pm X)$$

$$11) (G_2 [G_1(R - H_3 Y) - H_2 Y / G_4]) \cdot \frac{G_3 G_4}{1 - G_3 G_4 H_1} = Y$$

Isolando Y:

$$\frac{Y}{R} = \frac{G_1 G_2 G_3 G_4}{(1 - G_3 G_4 H_1 + G_2 G_3 H_2 + G_1 G_2 G_3 G_4 H_3)}$$

$$12) \text{ Seja } T = \frac{G_1 \cdot G_2 G_3 G_4}{1 - G_3 G_4 H_1 + G_2 G_3 H_2} \quad - \quad AT = Y$$

$$B = Y H_3$$

$$A = R - B = R - Y H_3$$

$$\frac{Y}{R} = \frac{R - Y H_3}{R}$$

$$Y = \frac{T}{1 + T H_3}$$

$$Y \left(\frac{1 + H_3}{R} \right) = R$$

$$\frac{1 + T H_3}{R}$$

$$T$$

$$13) \left| \frac{V}{R} = \frac{G_1 G_2 G_3 G_4}{1 - G_3 G_4 H_1 + G_2 G_3 H_2 + G_1 G_2 G_3 G_4 H_2} \right|$$