

1) Demonstramos que

$$\dot{m} = (C_v + C_c) \frac{dP_0}{dt}$$

onde $C_v = \rho \frac{dV}{dP_0}$ e $C_c = \frac{VM}{RT}$

Para o fole $V = Ax$, então

$$C_c = \frac{AM}{RT} x$$

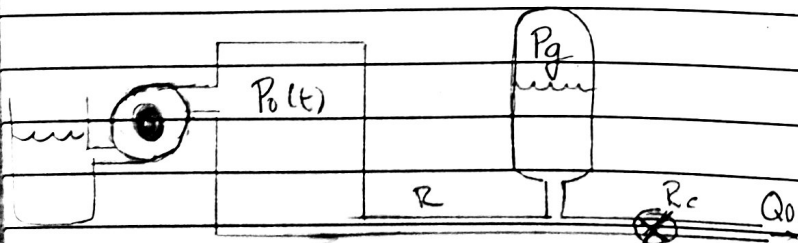
Temos, nesse caso, $V = 2m^3$, $T = 50^\circ C = 323,15 K$ e $R/M = 287 Nm/kgK$, donde

$$C_c = \frac{VM}{RT} = \frac{2}{287 \cdot 323,15}$$

$$C_c = 2,16 \times 10^{-5} ms^2$$

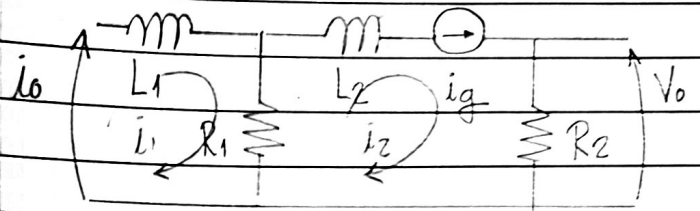
2) Hipóteses:

- reg. permanente
- líq. incompressível
- sist. adiabático
- reg. turbulento
- tubos de pequeno comprimento



Trataremos o ar como gás ideal mantido à pressão P_g constante.

a) $E_1 \begin{cases} Q \rightarrow V \\ P \rightarrow i \end{cases} \begin{matrix} R \rightarrow 1/pgR_f \\ L \rightarrow A/pg \end{matrix}$



Malha 1

$$L_1 D i_1 + R_1 (i_1 - i_2) = 0$$

$$(L_1 D + R_1) i_1 = R_1 i_2$$

$$\therefore \left(\frac{A_1 D + 1}{pg} \right) P_0 = \frac{1}{pg R_c} P_g$$

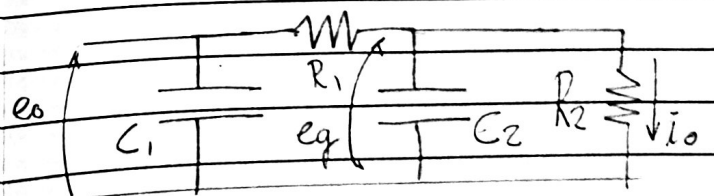
Malha 2

$$L_2 D i_2 + R_2 i_2 + R_1 (i_2 - i_1) = 0$$

$$\therefore \left(\frac{A_2 D + 1}{pg} \right) P_0 = \frac{P_g}{pg R_c}$$

Mas $V_0 = R_2 i_2 \rightarrow Q_0(t) = \frac{P_g}{pg R_c}$

b) $E_2 \begin{cases} P \rightarrow V \\ Q \rightarrow i \end{cases} \begin{matrix} R \rightarrow pgR_f \\ C \rightarrow A/pg \end{matrix}$



Nó 1

$$V_1 (C_1 D + 1/R_1) - V_2/R_1 = 0$$

$$P_0 (A_1 D/pg + 1/pgR) = P_g/pgR$$

Nó 2

$$V_2 (C_2 D + 1/R_2 + 1/R_1) - V_1/R_1 = 0$$

$$\frac{P_0}{pg} \left(\frac{A_2 D}{pg} + \frac{1}{pg R_c} + \frac{1}{pg R} \right) = \frac{P_g}{pg R} ; \boxed{P_g = pg R_c Q_0}$$