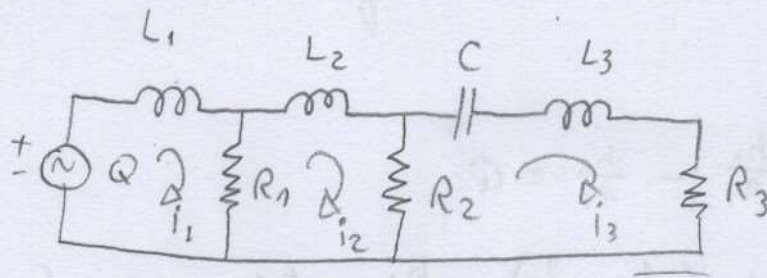


Modelagem de sistemas dinâmicos - Ex aula (22/09)

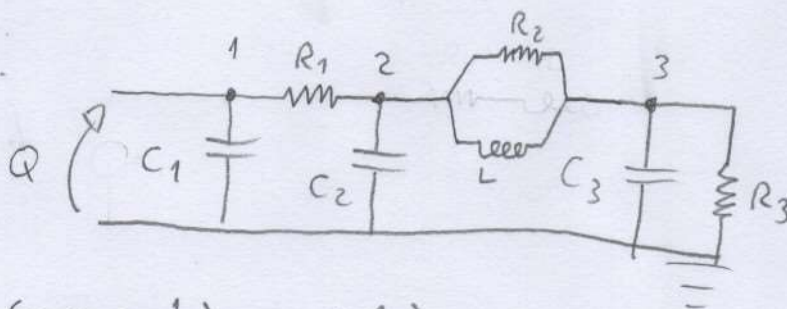
Exercício

Analogia 1:



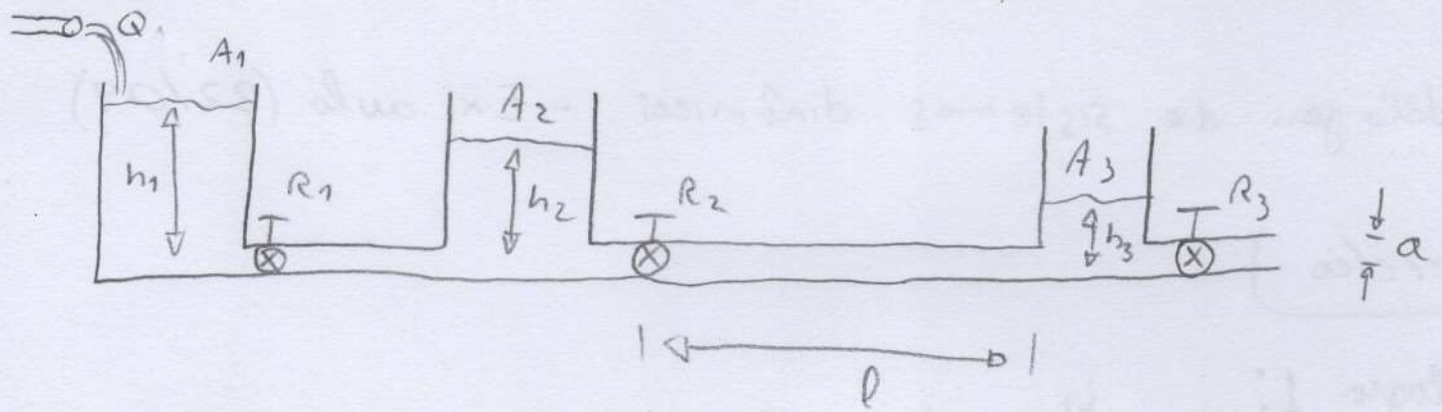
- Circuito 1: $i_1(L_1 D + R_1) - i_2 R_1 = Q$
- Circuito 2: $i_2(L_2 D + R_1 + R_2) - i_1 R_1 - i_3 R_2 = 0$
- Circuito 3: $i_3(L_3 D + R_2 + R_3 + \frac{1}{CD}) - i_2 R_2 = 0$

Analogia 2:



- Nó 1: $V_1(C_1 D + \frac{1}{R_1}) - V_2(\frac{1}{R_1}) = Q$
- Nó 2: $V_2(C_2 D + \frac{1}{R_1} + \frac{1}{R_2}) - V_1(\frac{1}{R_1}) - V_3(\frac{1}{R_2} + \frac{1}{LD}) = 0$
- Nó 3: $V_3(C_3 D + \frac{1}{R_2} + \frac{1}{R_3} + \frac{1}{LD}) - V_2(\frac{1}{R_2} + \frac{1}{LD}) = 0$

Reservatórios:



Reservatório 1: $A_1 \dot{h}_1 + \frac{h_1}{R_1} - \frac{h_2}{R_1} = Q$

Reservatório 2: $A_2 \dot{h}_2 + h_2 \left(\frac{1}{R_1} + \frac{1}{R_2} \right) - \frac{h_1}{R_1} - \frac{h_3}{R_2} + \frac{ga}{l} \int h_2 - h_3 dt = 0$

Reservatório 3: $A_3 \dot{h}_3 + h_3 \left(\frac{1}{R_2} + \frac{1}{R_3} \right) - \frac{h_2}{R_2} + \frac{ga}{l} \int h_3 - h_2 dt = 0$



$$Q = \left(\frac{1}{R_1} \right) V_1 - \left(\frac{1}{R_1} + \frac{1}{R_2} \right) V_2 + \left(\frac{1}{R_2} \right) V_3$$

$$0 = \left(\frac{1}{R_1} + \frac{1}{R_2} \right) V_2 - \left(\frac{1}{R_1} \right) V_1 - \left(\frac{1}{R_2} + \frac{1}{R_3} + \frac{ga}{l} \right) V_3$$

$$0 = \left(\frac{1}{R_2} + \frac{1}{R_3} \right) V_3 - \left(\frac{1}{R_2} + \frac{1}{R_3} + \frac{ga}{l} \right) V_2 + \left(\frac{1}{R_2} \right) V_1$$