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Exercício Aula 17/09/20.

1) Linearizar  $f(x) = \cos x$

$$\bullet f(x) = f(\bar{x}) + \left. \frac{df}{dx} \right|_{x=\bar{x}} (x - \bar{x}) + O^2$$

$$\bullet f(x) \approx f(\bar{x}) + \left. \frac{df}{dx} \right|_{x=\bar{x}} = \cos \bar{x} - \sin \bar{x} (x - \bar{x})$$

a. Para  $\bar{x} = 0$ :

$$\bullet f(x) \approx \cos 0 - \sin 0 (x - 0) = 1$$

$$\bullet f(x) \approx 1.$$

b. Para  $\bar{x} = \pi/4$ :

$$\bullet f(x) \approx \cos \pi/4 - \sin \pi/4 (x - \pi/4)$$

$$\bullet f(x) \approx \sqrt{2}/2 - \sqrt{2}/2 (x - \pi/4)$$

2) Linearizar  $f(\bar{v}, \bar{r}, \bar{r}, \bar{u}, \bar{x}) = -m\dot{v} - mr\dot{u} + m\dot{x}\dot{r} = -F(t)$

$$\begin{aligned} -F(t) \approx & f(\bar{v}, \bar{r}, \bar{r}, \bar{u}, \bar{x}) + \left. \frac{\partial f}{\partial v} \right|_{eq} (\dot{v} - \bar{v}) + \left. \frac{\partial f}{\partial r} \right|_{eq} (r - \bar{r}) + \left. \frac{\partial f}{\partial \dot{r}} \right|_{eq} (\dot{r} - \bar{\dot{r}}) \\ & + \left. \frac{\partial f}{\partial u} \right|_{eq} (u - \bar{u}) + \left. \frac{\partial f}{\partial x} \right|_{eq} (x - \bar{x}) \end{aligned}$$

• No equilíbrio temos:  $\bar{r} = \bar{\dot{r}} = \bar{v} = 0$

$$\begin{aligned} -F(t) \approx & f(\bar{v}, \bar{r}, \bar{r}, \bar{u}, \bar{x}) + [-m(\dot{v} - \bar{v})] + [-m\bar{u}(r - \bar{r})] + [m\bar{x}(\dot{r} - \bar{\dot{r}})] \\ & + [-m\bar{r}(u - \bar{u})] + [m\bar{r}(x - \bar{x})] \end{aligned}$$



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$$\therefore F(t) = m\dot{v} + m\ddot{u}r - m\ddot{x}r$$

$$m\dot{v} = m\ddot{x}r - m\ddot{u}r + F(t)$$